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Lab 3

Problem 1:

The purpose of problem 1 is to find the 3 keys/digits corresponding to our RUID. I saw that the blanking interval does not affect the result of decoding a signal. This is because where there is blanking, the values are zero so the frequency does not change. I had to convert between the frequencies from Hz to radians per sample in order to get the correct results for this problem.

Problem 1.1:

y = dtmfsig(179008726);

x = linspace(0, 0.9, 7200);

figure;

plot(x, y);

hold on;

xlim([0, 0.9]);

ylim([-3, 3]);

title("DTMT time signal");

hold off;



Problem 2.2:

fL = [697, 770, 852, 941];

fH = [1209, 1336, 1477];

fs = 8000;

fL = (2\*pi\*fL)/fs;

fH = (2\*pi\*fH)/fs;

first = y(1:2400);

second = y(2401:4800);

third = y(4801:7200);

fL1 = abs(freqz(first, 1, fL));

display(fL1);

fH1 = abs(freqz(first, 1, fH));

display(fH1);

fL2 = abs(freqz(second, 1, fL));

display(fL2);

fH2 = abs(freqz(second, 1, fH));

display(fH2);

fL3 = abs(freqz(third, 1, fL));

display(fL3);

fH3 = abs(freqz(third, 1, fH));

display(fH3);

first = y(1:1600);

second = y(2401:4000);

third = y(4801:6400);

fL1 = abs(freqz(first, 1, fL));

display(fL1);

fH1 = abs(freqz(first, 1, fH));

display(fH1);

fL2 = abs(freqz(second, 1, fL));

display(fL2);

fH2 = abs(freqz(second, 1, fH));

display(fH2);

fL3 = abs(freqz(third, 1, fL));

display(fL3);

fH3 = abs(freqz(third, 1, fH));

display(fH3);

With Blanking:

fL1 =

800.2524 14.5731 0.8751 1.6369

fH1 =

2.2222 4.2074 799.9657

fL2 =

19.0534 798.8779 11.7836 3.0972

fH2 =

798.5292 10.4165 5.8453

fL3 =

17.6748 800.3964 13.7706 4.3757

fH3 =

4.2039 5.5850 800.3260

Without Blanking:

fL1 =

800.2524 14.5731 0.8751 1.6369

fH1 =

2.2222 4.2074 799.9657

fL2 =

19.0534 798.8779 11.7836 3.0972

fH2 =

798.5292 10.4165 5.8453

fL3 =

17.6748 800.3964 13.7706 4.3757

fH3 =

4.2039 5.5850 800.3260

We see that with or without blanking does not matter and that the results are the same.

fL1 → The highest number is the first one which corresponds to 697

fH1 → The highest number is the third one which corresponds to 1477

fL2 → The highest number is the second one which corresponds to 770

fH2 → The highest number is the first one which corresponds to 1336

fL3 → The highest number is the second one which corresponds to 770

fH3 → The highest number is the third one which corresponds to 1477

Key1 = 3 Key2 = 5 Key3 = 6

Problem 1.3:

f = 600:1600;

f = (2\*pi\*f)/fs;

%key 3

dtft = abs(freqz(first, 1, f));

dialfreq = [fL, fH];

key3 = [fL1, fH1]/max(dtft);

figure;

plot(f, dtft/max(dtft));

hold on;

plot(dialfreq, key3, 'r.');

title('normalized spectrum of decoded key 3');

ax = gca;

ax.XTick = [697/8000\*2\*pi 1477/8000\*2\*pi];

ax.XTickLabel = {'697' , '1477'};

xlim([0.4712 1.2]);

ylim([0 1.2]);

hold off;

%key 4

dtft = abs(freqz(second, 1, f));

dialfreq = [fL, fH];

key4 = [fL2, fH2]/max(dtft);

figure;

plot(f, dtft/max(dtft));

hold on;

plot(dialfreq, key4, 'r.');

title('normalized spectrum of decoded key 4');

ax = gca;

ax.XTick = [770/8000\*2\*pi 1209/8000\*2\*pi];

ax.XTickLabel = {'770' , '1209'};

xlim([0.4712 1.25]);

ylim([0 1.2]);

hold off;

%key 6

dtft = abs(freqz(third, 1, f));

dialfreq = [fL, fH];

key6 = [fL3, fH3]/max(dtft);

figure;

plot(f, dtft/max(dtft));

hold on;

plot(dialfreq, key6, 'r.');

title('normalized spectrum of decoded key 6');

ax = gca;

ax.XTick = [770/8000\*2\*pi 1477/8000\*2\*pi];

ax.XTickLabel = {'770' , '1477'};

xlim([0.4712 1.25]);

ylim([0 1.2]);

hold off;







Problem 1.4:

f = [697 770 852 941 1209 1336 1477];

Table = [f; key3; key4; key6];

fprintf(' f | key 3 key 4 key 6\n');

fprintf('------|-----------------------------\n');

fprintf(' %4i | %7.3f %7.3f %7.3f\n', Table);

f | key 3 key 4 key 6

------|-----------------------------

697 | 1.000 0.024 0.022

770 | 0.018 1.000 1.000

852 | 0.001 0.015 0.017

941 | 0.002 0.004 0.005

1209 | 0.003 1.000 0.005

1336 | 0.005 0.013 0.007

1477 | 1.000 0.007 1.000

Problem 2:

The purpose of problem 2 is to see the change in the fundamental frequency after it has been through the discrete domain. I saw that the hamming weights had less noise when rectangular weight signals were used. Also, I tried to create an ideal reconstruction using the Butterworth analog lowpass filter. I also saw the differences of each frequency when put through different steps. The reconstruction stage showed very similar graphs for both frequencies.

Problem 2.1:

f0 = 0.125;

fs = 1;

M = -20:1:20;

fm = f0 + M\*fs;

t = 0:.01:20;

wm = 0.54 + 0.46\*cos((pi/20)\*M);

[tf, F] = meshgrid(t, fm);

[tw, W] = meshgrid(t, wm);

G = @(f) sin((pi\*f)/fs)./((pi\*f)/fs);

xa = cos(2\*pi\*f0\*t);

xr = sum(G(F).\*cos(2\*pi\*tf.\*F-pi\*F));

xh = sum(W.\*G(F).\*cos(2\*pi\*tw.\*F-pi\*F));

xp = G(f0)\*cos(2\*pi\*f0\*t-pi\*f0);

figure;

plot(t, xr, t, xp, t, xa);

hold on;

title('rectangular weights f\_0 = 0.125 kHz');

xlim([0 20]);

ylim([-2 2]);

hold off;

figure;

plot(t, xh, t, xp, t, xa);

hold on;

title('Hamming weights f\_0 = 0.125 kHz');

xlim([0 20]);

ylim([-2 2]);

hold off;

att = xp/xa;

attdB = -10\*log10(att);

display(attdB);

[c, i] = max(xp);

[d, j] = max(xa);

phase = i-j;

display(phase);





Attenuation in dB =

0.4560

Phase Delay =

50

We see that the attenuation and the phase delay is consistent with the graphs.

Problem 2.2:

f3dB = fs/2;

[b, a] = butter(6, 2\*pi\*f3dB, 's');

xf = lsim(b, a, xh, t);

figure;

plot(t, xf, t, xp, t, xh, t, xa);

hold on;

title('Post filter output, f\_0 = 0.125 kHz')

xlim([0 20]);

ylim([-2 2]);

hold off;

[maxxp, xpindex] = max(xp(800:1000));

[maxxf, xfindex] = max(xf(800:1000));

delay = (xfindex-xpindex)/100;

display(delay);

Hpost = @(g) polyval(b, 2\*pi\*1i\*g)./polyval(a, 2\*pi\*1i\*g);

exactdelay = (-atan2(imag(Hpost(f0)),real(Hpost(f0))))/(2\*pi\*f0);

display(exactdelay);



delay =

1.2600

Exact delay =

1.2395

Problem 2.3:

M = 0:1:3;

f = 0:0.01:4;

fm = f0 + M\*fs;

figure;

plot(f, abs(G(f)), f, abs(Hpost(f)), f, abs(G(f)).\*abs(Hpost(f)));

hold on;

stem(fm,abs(G(fm)),'b.');

title('reconstruction stages, f\_0 = 0.125 kHz')

hold off;

figure;

plot(f, abs(G(f)), f, abs(Hpost(f)), f, abs(G(f)).\*abs(Hpost(f)));

hold on;

stem(fm,abs(G(fm)).\*abs(Hpost(fm)),'r.');

title('reconstruction stages, f\_0 = 0.125 kHz');

hold off;





Problem 2.4:

f0 = 0.25;

fs = 1;

M = -20:1:20;

fm = f0 + M\*fs;

t = 0:.01:20;

wm = 0.54 + 0.46\*cos((pi/20)\*M);

[tf, F] = meshgrid(t, fm);

[tw, W] = meshgrid(t, wm);

G = @(f) sin((pi\*f)/fs)./((pi\*f)/fs);

xa = cos(2\*pi\*f0\*t);

xr = sum(G(F).\*cos(2\*pi\*tf.\*F-pi\*F));

xh = sum(W.\*G(F).\*cos(2\*pi\*tw.\*F-pi\*F));

xp = G(f0)\*cos(2\*pi\*f0\*t-pi\*f0);

figure;

plot(t, xr, t, xp, t, xa);

hold on;

title('rectangular weights f\_0 = 0.125 kHz');

xlim([0 20]);

ylim([-2 2]);

figure;

plot(t, xh, t, xp, t, xa);

hold on;

title('Hamming weights f\_0 = 0.125 kHz');

xlim([0 20]);

ylim([-2 2]);

att = xp/xa;

attdB = -10\*log10(att);

display(attdB);

[c, i] = max(xp);

[d, j] = max(xa);

phase = i-j;

display(phase);

f3dB = fs/2;

[b, a] = butter(6, 2\*pi\*f3dB, 's');

xf = lsim(b, a, xh, t);

figure;

plot(t, xf, t, xp, t, xh, t, xa);

hold on;

title('Post filter output, f\_0 = 0.125 kHz');

xlim([0 20]);

ylim([-2 2]);

hold off;

[maxxp, xpindex] = max(xp(800:1000));

[maxxf, xfindex] = max(xf(800:1000));

delay = (xfindex-xpindex)/100;

display(delay);

Hpost = @(g) polyval(b,2\*pi\*1i\*g)./ polyval(a,2\*pi\*1i\*g);

exactdelay = (-atan2(imag(Hpost(f0)),real(Hpost(f0))))/(2\*pi\*f0);

display(exactdelay);





Attenuation in dB =

1.9612

Phase Delay =

50



delay =

1.3000

Exact Delay =

1.2725

Problem 2.5:

% For f0 = 0.125

f0 = 0.125;

M =0:3;

fm =@(m) f0 + m.\*fs;

fm0 = fm(M);

gm0 = abs(G(fm0));

postf0 = abs(G(fm0).\*Hpost(fm0));

% For f0 = 0.25

f0 = 0.25;

fm =@(m) f0 + m.\*fs;

fm1 = fm(M);

gm1 = abs(G(fm1));

postf1 = abs(G(fm1).\*Hpost(fm1));

Table = [fm0; fm1; gm0; gm1; postf0; postf1];

fprintf(' fm = f0 + m\*fs | |G(fm)| | |G(fm)Hpost(fm)|\n');

fprintf('----------------|-------------------|---------------------\n');

fprintf('%7.4f %7.4f | %8.6f %8.6f | %8.6f %8.6f\n', Table);

fm = f0 + m\*fs | |G(fm)| | |G(fm)Hpost(fm)|

----------------|-------------------|---------------------

0.1250 0.2500 | 0.974495 0.900316 | 0.974495 0.900206

1.1250 1.2500 | 0.108277 0.180063 | 0.000835 0.000738

2.1250 2.2500 | 0.057323 0.100035 | 0.000010 0.000012

3.1250 3.2500 | 0.038980 0.069255 | 0.000001 0.000001

Problem 2.6:

fo = [0.125 .250];

td = [1.26, 1.30];

T0 = [1.2395, 1.2725];

T1 = -angle/(.7854);

T2 = -angle/(1.5708);

f = 0:.001:4;

angle = -atan2(imag(Hpost(f)),real(Hpost(f)))./(2\*pi\*f);

fprintf(' phase delay exact estimated\n');

fprintf('--------------------------------\n');

fprintf('fO =%6.3f | %6.4f | %6.4f \n', [fo(1:2);T0(1:2); td(1:2)]);

figure;

plot(f, angle, fo, td, 'r.', fo, T0, 'k.');

hold on;

title('reconstruction stages, f\_o = 0.25 kHz');

xlim([0 4]);

ylim([-1.6 1.6]);

phase delay exact estimated

--------------------------------

fO = 0.125 | 1.2395 | 1.2600

fO = 0.250 | 1.2725 | 1.3000



Problem 3:

The purpose of problem 3 is to compare X(Ω), T Xd(Ω), and T XM(Ω) for various values of T and M. For the first part of the problem we compare the difference when fs is 1Hz and 2Hz. The graphs look similar, but there are more sample points in fs = 2Hz. For the second part, we compare when the value of fs and M are changing. When fs is increased, the max and min becomes more like that of the analog signal. When M is increased, the replica signal is extended.

Problem 3.1:

a = 1;

fo = .5;

fs = 1;

wo = 2\*pi\*fo;

X = @(t) t.\*exp((-a\*t)+1i\*wo\*t);

t = 0:.001:8;

ts = 0:(1/fs):8;

figure;

plot(t, real(X(t)), ts, real(X(ts)), 'r.');

hold on;

title('x(t) = te^{-at}cos(\omega\_ot), f\_s = 1');

xlim([0 8]);

ylim([-0.4 0.3]);

hold off;

fs = 2;

ts = 0:(1/fs):8;

figure;

plot(t, real(X(t)), ts, real(X(ts)), 'r.');

hold on;

title('x(t) = te^{-at}cos(\omega\_ot), f\_s = 2');

xlim([0 8]);

ylim([-0.4 0.3]);

hold off;





Problem 3.2:

f0 = 0.5;

M = -1:1:1;

fs = 0.5;

f = 0:0.01:4;

omega = 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 0.5; M=1');

xlim([0 4]);

ylim([0 1.1]);

hold off;

%fs = .5, M = 2

f0 = 0.5;

M = -2:1:2;

fs = 0.5;

f = (0:0.01:4);

omega= 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 0.5; M=2');

xlim([0 4]);

ylim([0 1.1]);

hold off;

%fs = 1, M = 1

f0 = 0.5;

M = -1:1:1;

fs = 1;

f = (0:0.01:4);

omega= 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 1; M=1');

xlim([0 4]);

ylim([0 1.1]);

hold off;

%fs = 1, M = 2

f0 = 0.5;

M = -2:1:2;

fs = 1;

f = (0:0.01:4);

omega= 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 1; M=2');

xlim([0 4]);

ylim([0 1.1]);

hold off;

%fs = 2, M = 1

f0 = 0.5;

M = -1:1:1;

fs = 2;

f = (0:0.01:4);

omega= 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 2; M=1');

xlim([0 4]);

ylim([0 1.1]);

hold off;

% fs = 2, M = 2

f0 = 0.5;

M = -2:1:2;

fs = 2;

f = (0:0.01:4);

omega= 2\*pi\*f;

X = 1./(a + 1i\*(omega - 2\*pi\*f0)).^2;

[F, R] = meshgrid(f, M);

Xd = (1/fs)^2.\*exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)./(1-exp(a/fs).\*exp(-1i\*(omega-2\*pi\*f0)/fs)).^2;

Xm = sum(1./(a+1i.\*(2\*pi.\*F-(2\*pi\*f0)-(R.\*(2\*pi\*fs)))).^2);

figure;

plot(f, abs(X/max(X)), f, abs(Xd), f, abs(Xm));

hold on;

title('f\_s = 2; M=2');

xlim([0 4]);

ylim([0 1.1]);

hold off;











